SM3 4.1: Simplifying Rationals

For problems 1-6, simplify each rational expression. State any restrictions on x.

1)
$$\frac{35x}{7x}$$

$$2) \quad \frac{3x+12}{2x+8}$$

$$3) \quad \frac{x^2 + 7x}{x}$$

4)
$$\frac{18x^4 - 6x^2 + 9x}{3x}$$
 5) $\frac{8 + 2x}{2x^2 + 10x + 8}$ 6) $\frac{2x^3 + 13x^2 - 7x}{x^2 + 7x}$

5)
$$\frac{8 + 2x}{2x^2 + 10x + 8}$$

6)
$$\frac{2x^3 + 13x^2 - 7x}{x^2 + 7x}$$

Show that $\frac{x^3-6x^2-7x}{x^2+4x+3}$ is equivalent to $\frac{x^2-7x}{x+3}$ for most values of x. State which values of x cause the expressions to be not equivalent.

What is the simplest rational expression that represents the depth of a pond that is $\frac{3x^2-8x}{5x}$ meters deep?

9) What is the simplest rational expression that can represent the diameter of a circle that has a radius of $\frac{4x-8}{3x-6}$ centimeters?

10) What are the simplest rational expressions that can be used to represent the length and width, in inches, of a rectangle with sides that are $\frac{x^2-x-6}{x+2}$, $\frac{x^2+x-20}{2x+10}$, $\frac{6x^2-96}{48+12x}$, and $\frac{2x-6}{2}$ inches?